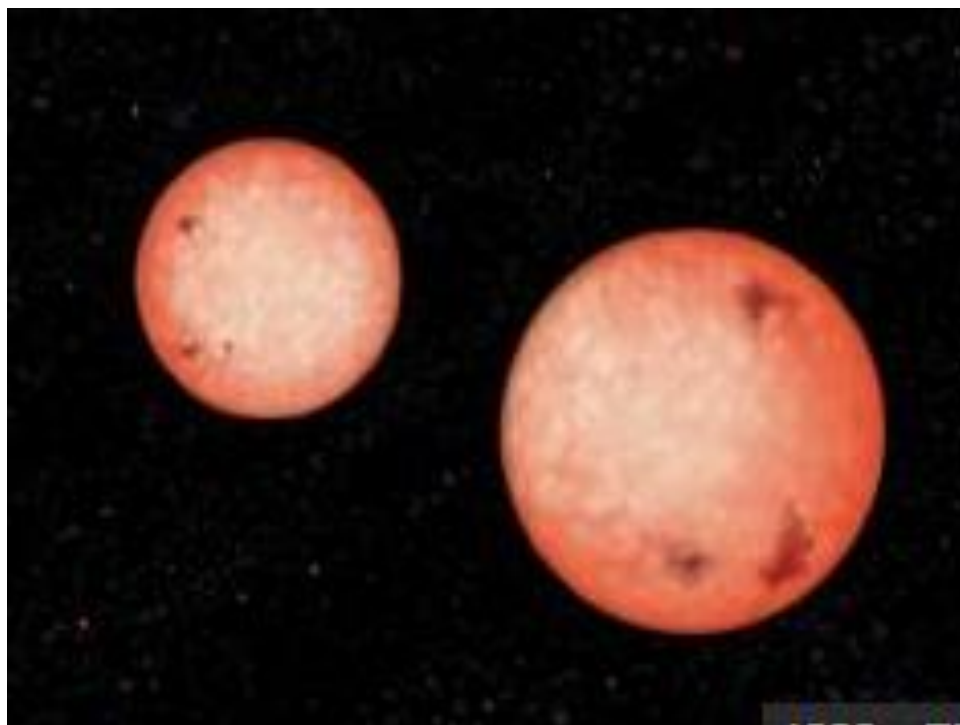
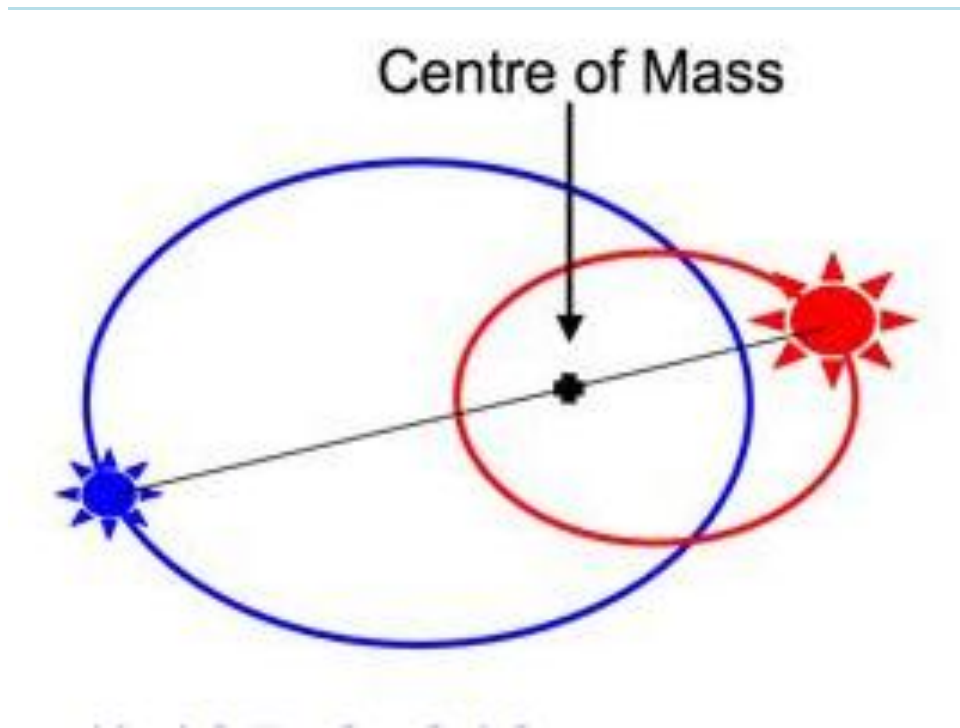


# Binary Stars

## Lecture 10







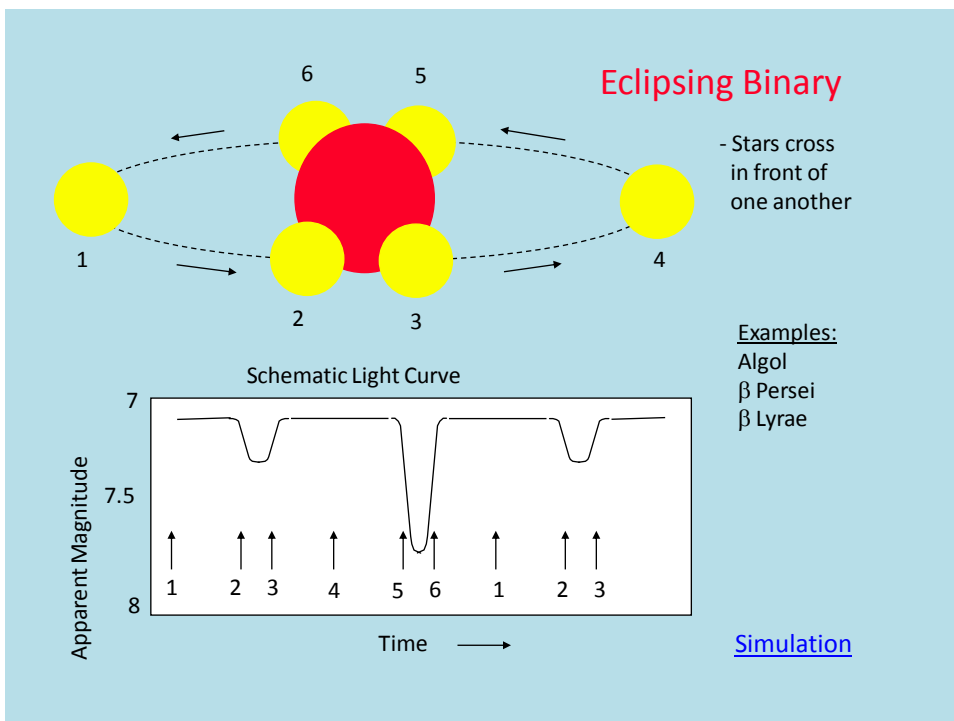
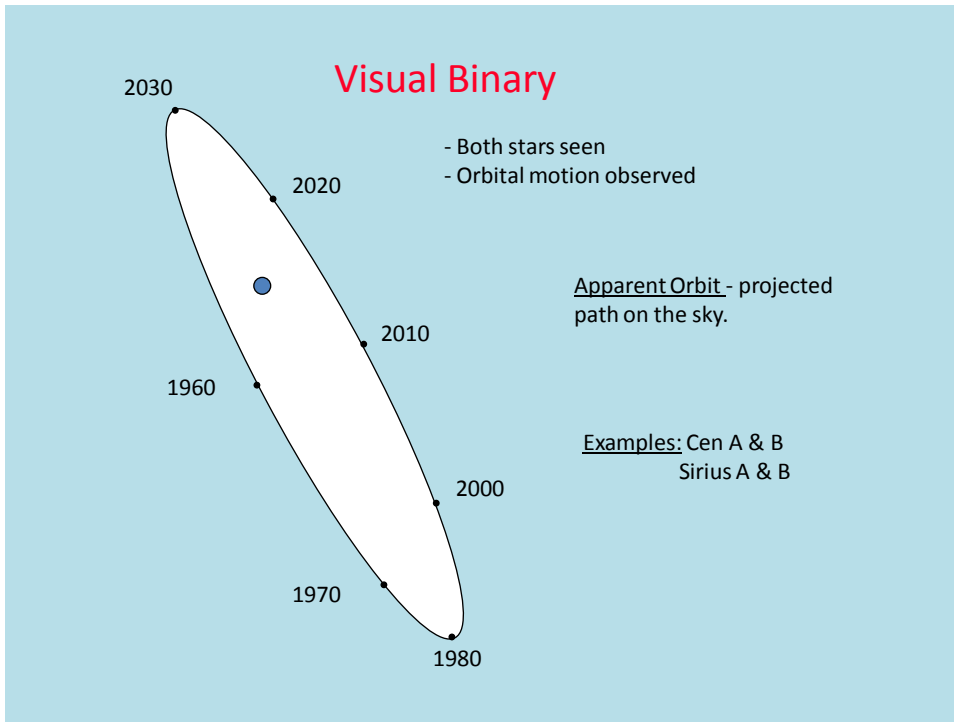
LIFE ON A PLANET  
IN A BINARY STELLAR  
SYSTEM

## Importance of Binary Stars

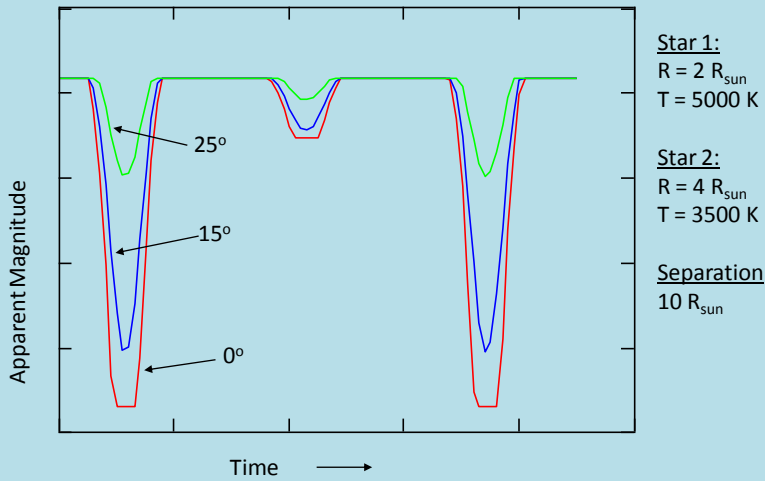
- 75 % of all stars are “binary stars”
- Studies give:
  - Stellar Masses (Visual & Spectroscopic)
  - Stellar Radii (Eclipsing)

## Types of binaries

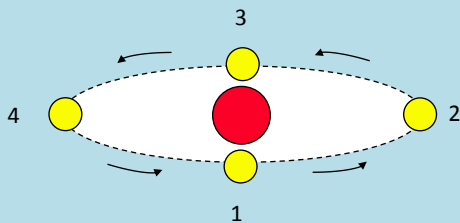
- Visual Binary
  - Stars are separated in a telescope.
- Spectroscopic Binary
  - See two sets of spectral lines Doppler shifted due to orbital motion.
- Eclipsing Binary (rare)
  - Stars cross in front of one another.



### Eclipsing Binary Light Curve



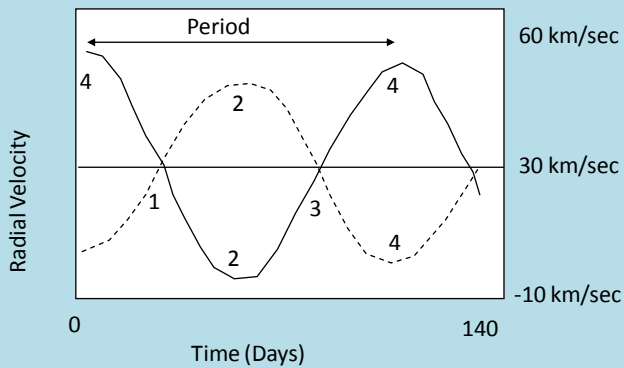
Angles are the orbital inclination.  $0^\circ$  is edge-on.



### Spectroscopic Binary

Doppler shift due to orbital motions.

Example:  $\beta$  Aurigae



## Masses of Binary Stars

- Newton's laws allow us to determine the total mass in a binary system.
- For star of mass  $M_A$  and  $M_B$ , the total mass is related to the period,  $P$ , and the average distance between the stars,  $a$ .

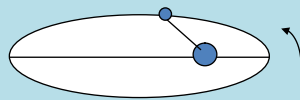
$$M_A + M_B = \frac{a^3}{P^2}$$

## Kepler's Laws of Planetary Motion

- They apply to binary stars
  1. Law of Ellipses
  2. Law of Areas
  3. Harmonic Law

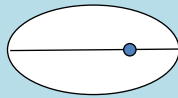
# 1. Law of Ellipses

- Orbits are ellipses

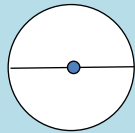


Eccentricity

$e=0.7$



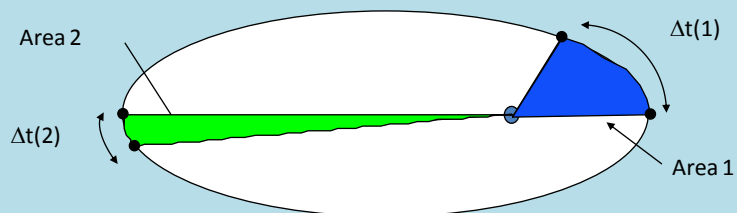
$e=0.4$



$e=0.0$  (circle)

# 2. Law of Areas

- Equal areas in equal time.

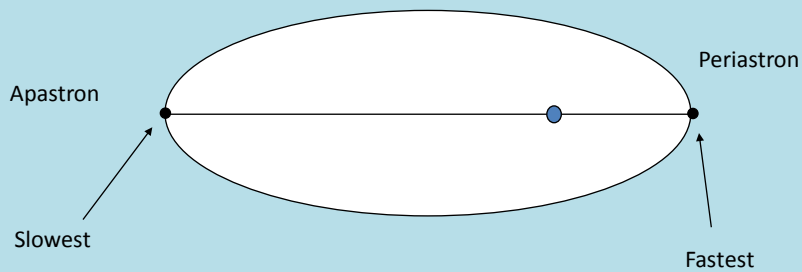


$$\Delta t(1) = \Delta t(2) \Rightarrow \text{Area 1} = \text{Area 2}$$



## 2. Law of Areas (continued)

- Orbital speeds



## 3. Harmonic Law

- (Orbital Period)<sup>2</sup> ∝ (Mean Distance)<sup>3</sup>

$$P^2 = \frac{a^3}{M_A + M_B}$$

- P = period of revolution in years
- a = mean separation in AU
- M<sub>A</sub> and M<sub>B</sub> = mass in solar masses

## Example:

- If a visual binary has a period of 32 years and an average separation of 16 AU then

$$M_A + M_B = \frac{16^3}{32^2}$$

$$M_A + M_B = 4 M_{\text{sun}}$$

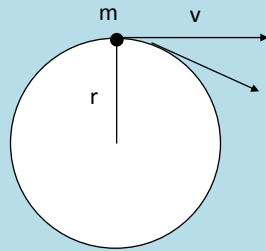
## Newton => Kepler !

- Deriving Kepler's third law
- Force = mass x acceleration

$$F = ma$$

- Acceleration is change in velocity with time.
- Force in Newtons.

## Circular Motion



$$\text{Acceleration} = \frac{v^2}{r}$$

$$\Rightarrow F = ma = m \frac{v^2}{r}$$

This is the (centripetal) force necessary to keep the mass in a circular orbit.

## Newton's Gravity

$$F = \frac{GMm}{r^2} \quad \text{but} \quad F = ma = m \frac{v^2}{r}$$

$$\Rightarrow \frac{GMm}{r^2} = \frac{mv^2}{r}$$

So that

$$v^2 = \frac{GM}{r}$$

## Putting it together

- The velocity and the orbital period,  $P$ , are related.  
The circumference is  $2\pi r$ , so

$$\Rightarrow P = \frac{2\pi r}{v} \quad \text{or} \quad v = \frac{2\pi r}{P}$$

Thus

$$v^2 = \frac{4\pi^2 r^2}{P^2} = \frac{GM}{r} \quad \Rightarrow \quad P^2 = \frac{4\pi^2}{G} \frac{r^3}{M}$$

Or  $P^2 \propto r^3$  **Kepler's Third Law!**

## Orbital Elements

- Apparent Orbit - as seen on the sky
- Real Orbit
- Size of major axis
- Eccentricity of Orbit
- Period of Revolution
- Orbit orientation angle
- Inclination of Orbit

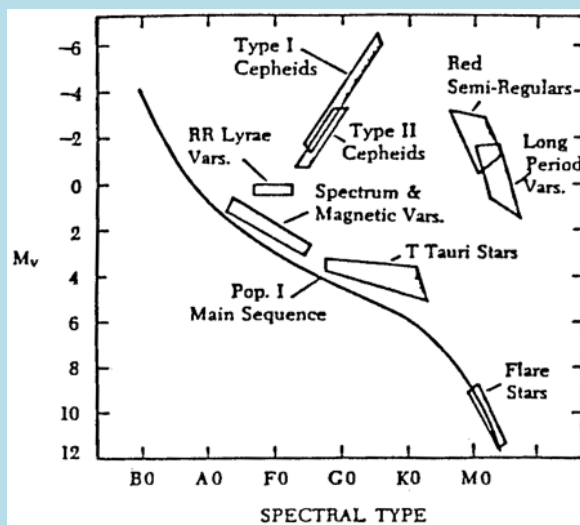
## Notes on binary masses

- Don't mistake the mass for magnitude!
- P is measured in years, a in AU and mass in solar masses in this formula.

$$M_A + M_B = \frac{a^3}{P^2}$$

- We can only get the total mass.

## Variable Star Classes



## Pulsating Variable Stars

Type	Period	Mag. Change	Spectrum
Classical Cepheids (I)	2-80 days	1	F, G Supergiants
Type II Cepheids	1-100 days	1	F, G, K giants
Long Period Variables	90-600 days	3-6	M giants
RR Lyrae	1-24 hr	1	A, F giants
Canis Majoris	3-6 hr	0.1	B
Semiregular	~ 100 days	1	M
Irregular	irregular	1-6	G, K, M

## Period Luminosity Relation

